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Pedestrian monitoring system for indoor billboard evaluation

Thomas Liebig [1,2]* and Zhao Xu [2]

[1] *University of Bonn, Bonn, Germany*
[2] *Fraunhofer IAIS, Sankt Augustin, Germany*

Abstract. Recent event monitoring, safety planning and location evaluation applications require models of pedestrian movements as well as monitoring of their presence. These indispensible insights have to be integrated in larger software systems seamlessly. In this work we propose a pedestrian monitoring system which supports these applications by a novel, robust analysis method based only on few empirical measurements. The gathering of empirical data on pedestrian movement and its analysis are combined via Open Geographic Consortium (OGC) compliant protocols. This utilizes usage of heterogeneous movement sensors, as well as fast integration of the analysis results in other applications. We demonstrate our novel method in an industrial billboard performance evaluation use case. Whereas for billboard evaluation a handful of pioneer countries trace personal mobility now via GPS devices, GPS technology has the drawback that it cannot be applied indoors due to signal loss. In Switzerland and Germany many valuable posters are situated in public buildings such as train stations or shopping malls and their evaluation is of high interest. In this paper we therefore present a new approach for the evaluation of mixed indoor-outdoor campaigns. Our pedestrian monitoring system is applied to denote at once quantities and trajectories of the people in restricted spaces based on empirical movement observations. Our approach has been implemented for 27 major train stations in Switzerland and was integrated in a system which evaluates performance of billboard mixed indoor/outdoor advertisement campaigns.

Keywords: pedestrian flow; billboard evaluation; regression

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Introduction

One of the most typical advertising media is billboard advertisement, which still plays an important role in contemporary advertisement mixtures. This is supported by its turnover of 684 million CHF (about 460 million Euro) 2008 in Switzerland and 805 million Euro in Germany (SWS 2009, FAW 2009).

Nevertheless, due to the competition with other media (including television, radio and press) and the emergence of digital and online media the market changed rapidly in recent years. To become incorporated by media planners in an advertisement mixture, transparent measures are needed to quantify the performance of a campaign. Typical measures include (1) the coverage or reach of a campaign, which is the percentage of persons within a target group defined by socio-demographic attributes that has contact with a campaign in a certain time interval (often one week) and (2) the number of contacts this group has. Improved methods for audience measurement have become available in the last years due to technical advances and improved methodology. For example, GPS technology

* *Correspondence*: Thomas Liebig, Fraunhofer IAIS, Schloss Birlinghoven, 53757 St. Augustin, Germany.
E-mail: thomas.liebig@iais.fraunhofer.de

has established itself as a new standard in Switzerland and Germany, greatly improving the possibilities of fine-grained media planning (May *et al* 2009, Pasquier *et al* 2008).

This paper focuses on the large amount of billboards which are situated at places where no GPS signal is available and other methods of traffic monitoring need to be developed. These places include for example airports and train stations as well exhibition centers. The performance of these poster locations is highly interesting for media planners because they are considered among the most valuable ones. We will investigate the special case of inner train-station campaigns in Switzerland in this paper, which covers 2,600 poster locations. We present in this work a novel Pedestrian Monitoring System (PMS), which we apply to compute pedestrian flows and quantities for the major Swiss train stations. This utilizes evaluation of the campaigns within the biggest 27 Swiss train stations. The challenge, we are going to tackle with the PMS, is to give an easy to integrate, general and flexible framework to answer the questions: Where do how many people move and which paths are used?

Tracking pedestrians with cameras, which might produce sufficient empirical data to answer this question and seems to be a perfect choice at the first sight, is often not permitted in train stations because of privacy restrictions and required scaffoldings. Radio Frequency Identification (RFID) and Bluetooth (Alt *et al* 2009, Liebig and Kemloh Wagoum 2012) technology may also be used for tracking, but this becomes expensive and requires an additional infrastructure for deployment of the necessary hardware. Another option for trajectory recording are interviews. However, they are very time consuming and thus expensive.

Our approach is based on low-cost measurements of pedestrian quantities at predefined locations that return the number of pedestrians passing by within a fixed time-slice. Although we are focusing on pedestrian analysis within train stations in this paper (which are comparable small), the presented system is flexible to support also for other pedestrian monitoring scenarios. The pedestrian flow model needs to be (1) adjustable by measurements of peoples quantity in order to represent the movement in the public building. Additionally, another requirement is (2) fulfillment of the Kirchhoff-laws at each crossing. This means that the number of incoming equals the number of outgoing people for any closed boundary.

These requirements are challenging to existing micro-scopic simulation models (see the next section) due to their difficult adjustability by empirical data (Kretz and Schreckenberg 2006). Our approach is based on regression approaches (Pushkarev and Zupan 1971, Tanyimboh and Templeman 1993, Yassin-Kassab *et al* 1999) that are so far used for quantity estimation. We extend the regression by a micro-scopic, i.e. path-based, pedestrian model in order to encode quantities and trajectories as required by the billboard evaluation task. The method we present is applicable in practice and was successfully applied to the 27 biggest Swiss train stations as part of an industrial application. Additionally, we integrate our method in a general Pedestrian Monitoring System (PMS) workflow that allows for fast deployment and application of the introduced analysis.

The paper is structured as follows. In section 2 we discuss related work. Next we describe in section 3 our pedestrian monitoring system and highlight its properties, and benefits. Section 4 addresses this industrial application: Motivated by reach estimation we estimate pedestrian trajectories and quantities for Zurich central station. We conclude with a section on future work.

Related Work

To the best of our knowledge, previous work concerning poster campaign evaluation only deals with outdoor campaigns. For the estimation of traffic flows in general a number of methods and algorithms exist in the literature. Initially being an operation research problem concerned with logistics and transportation issues, with increasing map-sizes it became a problem for spatial data mining. First, there exists a large group of probabilistic micro-simulation models including Monte Carlo methods (Borgers and Timmermans 1986), Markov models (Yu *et al* 2003), cellular automata (Blue and Adler 2001) and multi agent simulation (Rindsfüser 2005). These models describe individual pedestrians and model their behaviour within the spatial manifold, which could be represented by discrete variables as done by the cellular automata model or continuous variables as, for example, required by the social force model (Helbing 1997). The advantage of these microscopic models is that they allow including socio-demographic attributes and thus varying types of movement behaviour out of the box. Furthermore, they directly return individual trajectories, the macroscopic traffic features (e.g. quantities and densities) become derived afterwards.

Second, there are large-scale macro-scopic algorithms for traffic quantity prediction in (extensive) road networks (May *et al* 2008) as well as macro-scopic models that are based on gas and fluid-dynamic processes (Helbing

1997). These models return desired traffic quantities but no individual trajectories. Whereas the scope of the first model (May *et al* 2008) is just on prediction of quantities (there called: frequencies) the latter (Helbing 1997) is time-dependent and models multiple aspects of macro-scopic traffic features as functions over space x and time t, e.g. quantities $q(x,t)$, densities $\rho(x,t)$, velocities $v(x,t)$. Based on this notation, figure 1 gives a comparison of the micro-scopic and macro-scopic view on pedestrian movement.

Each of these models and algorithms makes certain assumptions on the mobility behaviour or path choices, reflecting different aspects of real-world traffic. Thus, model selection depends mainly on the application. Micro-simulation models are useful for evacuation planning and obstacle detection. Macro-scopic approaches are used to plan traffic control systems and to simulate the influence of infrastructural changes.

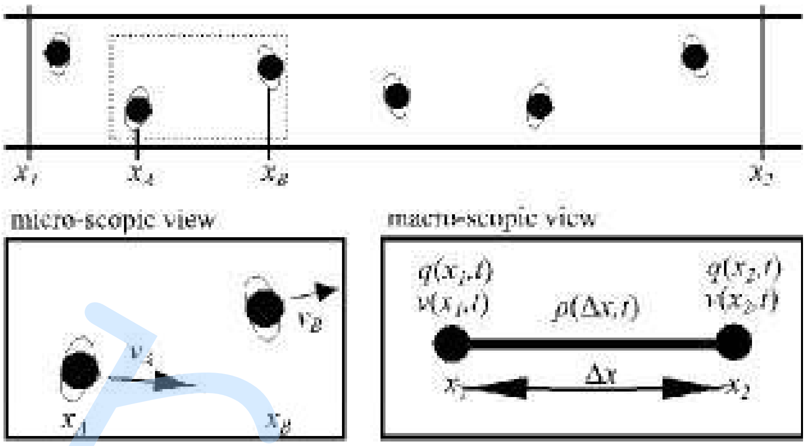

Fig. 1. macro-scopic and micro-scopic view on traffic

Pedestrian monitoring Ssystem (PMS)

In previous sections we motivated the questions for (1) quantity of persons among corridors and paths and (2) which routes they choose (section 1). We presented state-of-the-art approaches and highlighted their drawbacks (section 2). In summary, the mentioned requirements for industrial application of a monitoring algorithm include:

- fulfillment of Kirchhoff's law at any junction,
- usage of topological floor plan information instead of high-granular maps,
- adjustability by empirical measurements,
- robustness against noisy measurements and
- calculation time does not depend on number of monitored pedestrian movement.

In this section, we present how we tackle the task by a novel regression method which is embedded in a pedestrian monitoring system workflow to provide additional benefits, namely:

- integration of monitoring results in subsequent analysis and reporting tools,
- possible integration in real-time systems and
- seamless usage of heterogeneous sensor technologies.

Workflow

The Data Mining Process Model (Fayyad *et al* 1997) consists of three consecutive steps for data evaluation. Starting with raw input Data, the performed steps to achieve useful information are (1) Data Preprocessing, (2) Data Mining and (3) Post-processing. The presented Pedestrian Monitoring System (figure 2) encapsulates these steps in three layers: (1) The *Sensor Layer* which monitors people's movements and returns the geo-located information to the next layer. Depending on the application-specific requirements, varying sensor technologies can be integrated seamlessly to the monitoring layer by use of standardized Open Geographic Consortium (OGC) (http://www.opengeospatial.org, accessed 29 February 2012) interfaces for data transfer. (2) The *Query Layer* is used to interact with the user, who could ask for analyses within a given region and a certain time interval. These queries trigger the (3) *Analysis Layer* which performs the flow estimation. Results are returned to the user in format of the OGC conform Geography Markup Language (GML) (http://www.opengeospatial.org/standards/gml, accessed 29 February 2012) and may be processed further in Visual Analytics Toolkits (http://geoanalytics.net/ and, accessed 30 September 2011) and Geographic Information Systems (GIS). The layer structure is illustrated in figure 2.

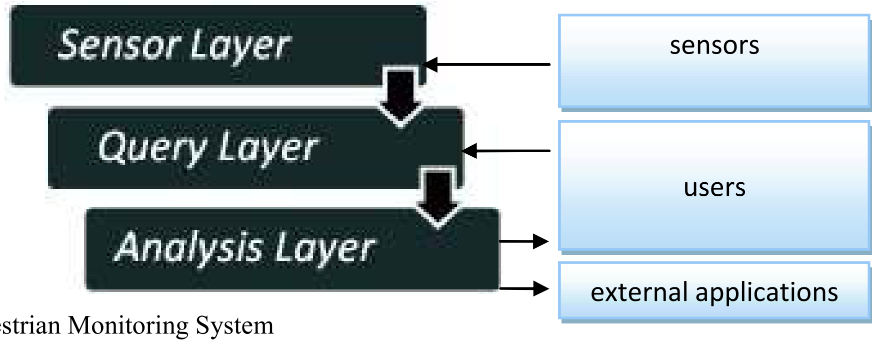

Fig. 2. Layers of the Pedestrian Monitoring System

Sensor Layer

Fetching raw empirical data on people's presence or movements is done in the *Sensor Layer*. The data of multiple arbitrary sensors is provided through a unique, standardized and open interface, namely, the sensor observation service (SOS) protocol (http://www.opengeospatial.org/standards/sos, accessed 30 September 2011), which is a XML standard for data collection from heterogeneous mobile sensors. Core functions of this Open Geographic Consortium (OGC) (http://www.opengeospatial.org, accessed 30 September 2011) standard are:

- GetCapabilities - used in order to achieve information on the monitored value,
- GetObservation - used to fetch measurements and
- DescribeSensor - returns ID and unit of observed value.

Possible pedestrian quantity sensor technologies are manual measurements, video surveillance, Radio Frequency Identification (RFID) and Bluetooth (Alt *et al* 2009). However the data is recorded, the retrieved values become transferred OGC compliant and stored in a Database for later consideration, when the *Query Layer* (respectively the user) asks for creation of pedestrian models based on historical data.

Query layer

The *Query Layer* provides an interface (to external applications or) to the analysis expert. He may decide for a specific spatial-temporal interval for analysis. This decision triggers the data *Analysis Layer* and defines its most important parameters. Analysis Results are handed back using the OGC compliant Geography Markup Language (GML) standard. The *Query Layer* supports real-time pedestrian monitoring solutions based on the continuously sensed data by regular triggering.

Analysis layer

Some of the pedestrian models presented in Section 2 require detailed representations of the accessible space. Applications for such models are emergency and evacuation planning, capacity analysis or obstacle detection. As we are only interested in quantities and paths to identify co-visits of locations, we do not require such a detailed model. Therefore, a directed graph approximation of the floors, stairways and junctions contains enough information for our task.

Every junction is represented by a vertex and the connecting floors are represented by pairs of edges and its opposite direction. Paths through the station may then be described by a sequence of edges, starting and ending at an entrance or platform. Quantities denote the number of people passing a certain edge within a fixed and pre-specified time-interval. The presented model focuses on presence of pedestrians and thus may disregard temporal aspects of movement.

Combined with the requirement to hold Kirchhoff's-laws at any junction the modeled time window needs to be chosen appropriate. As nobody lives within public buildings or starts to reside there permanently, the traffic for one day may be considered to hold Kirchhoff, for all edges adjacent to any arbitrary (but fixed) vertex.

Empirical recordings of pedestrian presence denote quantities plus some noise at pre-selected edges. Since the quantity of persons at a position is given by the number of people walking on each connected path that passes that location our approach consists of three steps: (1) The enumeration of the set of all valid paths, afterwards (2) the computation of path frequencies such that the error at the measured locations becomes minimized and, (3), the estimation of the number of people per edge. The three generated output variables edge-frequencies, path-frequencies and the path set are going to hold the desired information to answer the billboard campaign evaluation task (see section 4 for details). By the observation, people prefer routes with the minimal detour most, when walking from a given start to a target (Rindsfüser 2005), the assumption that most trajectories are un-cyclic is reasonable for public buildings. Empirical observation, we made during the application (section 4), also supports this assumption. We consider cyclic paths to be irrelevant for our study. Therefore, the path set becomes enumerable, utilizing the previous annotation of edges. By application of a characteristic function for each path, we construct for all paths its corresponding binary representation (vector) of constant length. Every position in the vector relates to an edge. The vector equals one at a position if the related edge is element of the path and is zero otherwise.

The program we solve in step (2) is then derived directly. We search the path frequency distribution whose edge-vise aggregates minimize the difference to the empirical data at the measurement locations. The objective function includes an additional term, which represents the preference of pedestrians to choose routes from start to goal in a detour avoiding manner (Rindsfüser 2005). This term not just penalizes detours, but has the advantage to make a specific solution more invariant on the used solver, because it further restricts the set of possible solution. The number of people per valid path that traverses the train station, computed in the previous step, is used to compute edge quantities for all locations in the station covered by valid paths which contain at least one measurement. The goal of the flow estimation was the calculation of the number of persons per position and a quantity distribution among their chosen paths. Both is given in result by our method and stored in the path set the edge frequencies and the path frequencies. The next section discusses its properties. An application to the industrial case is described.

Robustness

Due to the nature of empirical measurements they include small deviations. Thus, the combination of these counts in target quantities must lead to contradictions. As the measurements distinguish movement directions, the contradictions can be easily recognized it the raw data by violations of Kirchhoff's law at junctions, whereby the number of incoming people has to equal the number of the outgoing ones. In general, this problem may arise along multiple junctions. In this case, it is harder to pre-identify the contradictions. Therefore, we require the frequency estimation algorithm to recognize such cases automatically and to eliminate them in the model, if required. Our approach fulfills all of these criteria. The Kirchhoff law holds automatically, because the enumerated path set does: Every single path holds the constraint at any junction that the number of incoming people equals to the number of outgoing ones. Multiplying with the path quantities, our algorithm increases the number of people on this path, but nevertheless the equilibrium remains fulfilled. If each single route fulfills this constraint, the set of all paths including their final quantities also does. Therefore, in our pedestrian model Kirchhoff's law holds. From this property follows directly an invariance of the method on graph homeomorphisms for the traffic network. This means, if an edge becomes divided into two connected parts the resulting quantities remain the same. Kirchhoff's law ensures that all quantities are equal. Furthermore, the small perturbances included in the countings are corrected by the least squares regression. Without the need for a pre-analysis of outliers the resulting quantities are chosen such that the differences at the measurement locations are minimal.

Complexity

One weakness of micro-scopic models discussed in Section 2 is their poor adjustability by empirical traffic observations (Kretz and Schreckenberg 2006). This existing method cannot be used, as it requires a repeated execution of the whole simulation and an adjustment of the parameters. The time-complexity of each simulation run depends on the number of pedestrians and the length of the explored time-interval. In contrast, our ansatz scales well and does not depend on number of pedestrians nor the chosen time-interval, but the size of the station and the number of sensors. This property is important in the industrial case, where we made calculations for the 27 major train stations, including some with a daily usage of several hundred thousand passengers per day.

Real world application on Zurich central station

The motivation to investigate the questions for both (1) pedestrian quantities and (2) paths at the same time was given by an industrial use case, namely the performance evaluation of indoor poster campaigns. Thus, we successfully applied the method to the 27 major Swiss train stations. Within this section we illustrate the process for one example: Zurich central station. It highlights the advantage of the proposed method combining the calculated model with existing outdoor poster campaign evaluation approaches.

Pre-Pocessing and empirical data collection

The data we base our analysis on are a floorplan image and a few empirical recordings of pedestrian quantities at pre-selected locations. Before the previously presented monitoring system (section 3) can be applied, a required pre-processing step, is the tessellated of the floorplan by a traffic network representation as follows: Junctions are represented by vertices which then forms the vertex set. The connecting floors are represented by directed edges (each paired with its reverse). Entrances become annotated in this directed flow graph by edge attributes.

After doing a pre-study, we concluded that counting the number of people manually at several positions (using a smart phone application for data entry) is the most cost-efficient method for data collection. As noted in the introduction, using video cameras was not feasible because of privacy constraints. To decrease the influence of the day of week on the measurements, we repeated the measurements at three different days. As the number of "sensors" is limited, we had to select locations for counting in advance using the traffic network of the train stations. Therefore we located sensors at the most important junctions and stairways. Figure 2 depicts the measured edges at Zurich central station.

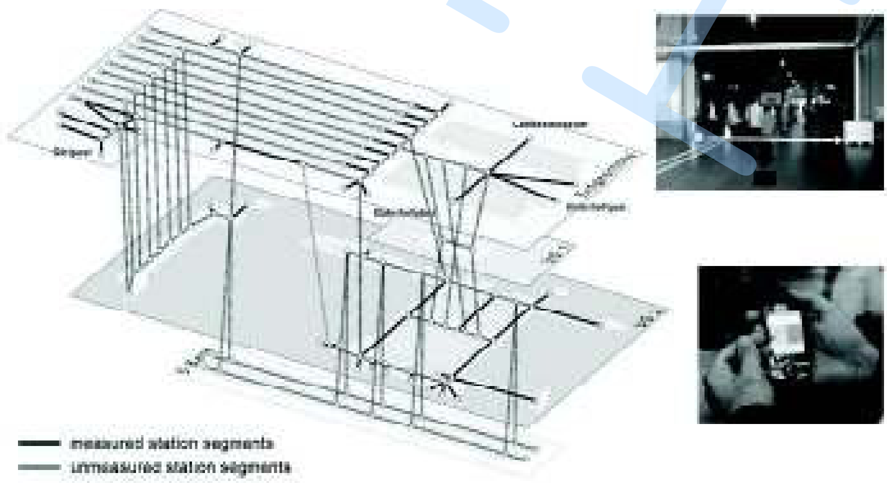

Fig. 3. Measurement locations in Zurich central station

To assist manual counting and to simplify post-processing of measurements, we developed a smart phone application (figure 3) which records clicks of the surveying person - each click represents the number of pedestrians passing in a specified direction - along with its timestamp. This enables easy integration of the measured data in the monitoring system as part of the *Sensor Layer*. Thus, we know how many people passed at which time into which direction. In an early prototype, we encountered the problem of mixed directions; therefore we added visual hints to the smartphone application as well as to the map. To distinguish directions, the colours red and green are used in our application.

To be able to compare the empirical raw data of pedestrians at measurement locations, e.g. an average number of pedestrians for a complete day or week, post-processing is necessary: after merging the measurements, the counted quantities are weighted and aggregated according to the time interval and day they were taken. As a result, every measured location in the train station has associated with it a number of pedestrians that may be compared against any other location. This is important for ranking locations or tracking segments within the building, which is a first feature of our Pedestrian Monitoring System.

Flow Estimation

For segments where empirical measurements have been taken, the quantities are known. Triggered by the *Query Layer*, our task is now to estimate them for the unobserved segments, and to build a pedestrian indoor movement model that is useful for poster and campaign evaluation within the selected time period.

In contrast to other regression models (Pushkarev and Zupan 1971, Tanyimboh and Templeman 1993, Yassin-Kassab *et al* 1999) that do not give paths but just frequencies, we tackle both questions at the same time, using a two stage regression approach. In a first step, we enumerate all plausible routes through the building and collect them in a route set. For example, at the main station in Zurich, there are about 380,000 conceivable routes. Non-plausible routes are eliminated, among them circular routes. Afterwards, we assign frequencies to each route, based on the measurements. The measurements serve as frequency targets in this process. The purpose of this assignment procedure is to find the optimal combination of routes that fulfills all frequency targets. As a result we obtain for every modeled train station (1) a set of routes crossing that station and (2) the number of people walking on each route. Figure 3 gives an example for Zurich central train station. With this information we are able to calculate quantities for each edge in the station by summing over route quantities, no matter whether the edge x_i has been measured empirically or not. This yields the pedestrian movement model based on empirical measurements we aim for. It enables us to denote pedestrian quantities at any location and gives trajectories also at unobserved segments.

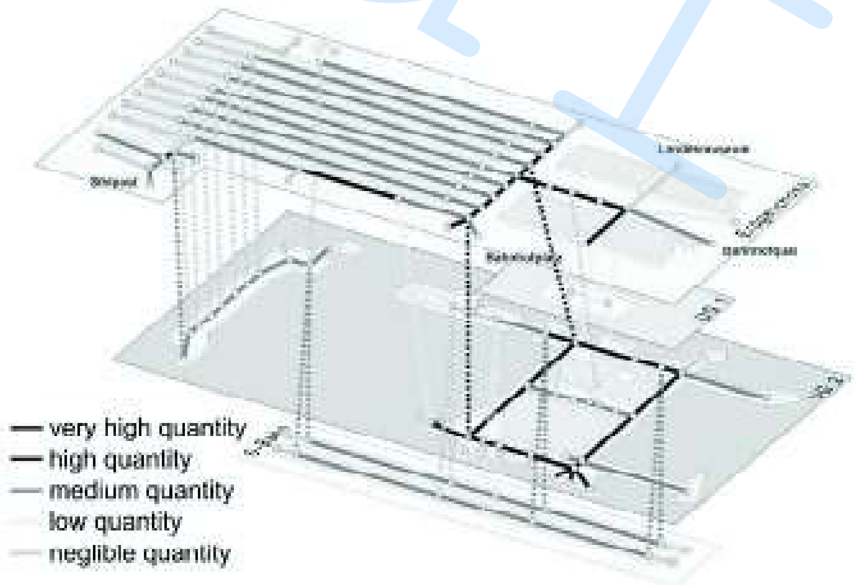

Fig. 4. Estimated quantities in Zurich central station

Integration with GPS surveys

In order to apply our pedestrian monitoring system for the evaluation of mixed indoor-outdoor poster campaigns, we still need to integrate it with GPS mobility data as mentioned in the introduction. This means, we have to re-use the output of the *Analysis Layer* and assign for each GPS person who enters a railway station a corresponding route through the station. To achieve this goal, we need to perform three subsequent steps: (1) visit identification, (2) route assignment and (3) performance evaluation.

In the first step we identify all test persons within the GPS sample visiting a train station. Based on GPS trajectories of over 10,000 test persons recorded over a period of one week per person, we isolate all tracks in the vicinity of a train station using buffers and the spatial join operation "intersect". As GPS signals may be noisy, we apply an individually sized buffer to each of the train station geometries, reflecting its specific local setting. The resulting candidate set, however, contains not only potential rail travelers but also regular pedestrians, car drivers and passengers passing by the station without entering it. We therefore apply a complex multi-level filtering process which identifies the visitors of a train station using, for instance, speed curves, the course of movement and time spent inside the geometric extension of the train station. Knowing all visits to a railway station completes step one.

Step two is the assignment of each visit to one of the routes underlying the pedestrian movement model. The challenge of this task is to find an optimal distribution of personalized routes given the route frequencies. We do this iteratively by drawing routes from the route set and considering the projected weight and socio-demographic information of each test person being assigned to that particular route. At the end of this step each GPS trajectory containing a visit to a train station, as identified in the previous step, has been assigned a route through the corresponding train station.

Finally in step three we weight poster contacts and calculate performance measures of mixed in- and outdoor campaigns. Similar to the performance evaluation of outdoor posters, we consider individual visibility criteria at each poster site. Routes passing the visibility area are weighted according to the contact quality, depending e.g. on the viewing direction or clustering of panels. Given weighted contacts for each indoor poster and visiting person, we can estimate total contacts and reach of a mixed indoor-outdoor campaign using the same algorithmic background as for outdoor campaigns. The selection of a campaign and of a target audience depends on all relevant (indoor and outdoor) poster contacts and the application of Kaplan-Meier compensates for missing measurement days in the GPS data as described in (Pasquier *et al* 2008).

Conclusion and future work

In this paper we developed a workflow that allows performance measurements for billboards that are placed indoors. We focused on 2,600 poster sites in railway stations as those are being seen as one of the most valuable over all. The challenge results from GPS signal loss inside buildings. Our proposed pedestrian monitoring system includes the development of a pedestrian model based on empirical data. This mobility information has been integrated with existing GPS mobility data, allowing to infer reach values and weighted contacts. We applied our approach to 27 major Swiss train stations.

Although we showed how to implement a general movement model within the train station which is used for poster campaign evaluation, we do not model time, so far. Our indoor model is static for the considered time period. Whereas this is al-ready sufficient for current billboard evaluation, continuous triggering of the analysis in a real-time scenario could be used for pervasive advertisement evaluation.

In the future, modeling pedestrian flow with Gaussian Processes enriched with relational data sources, as train schedules or text messages like news tickers, is a promising method. It will enhance our method and allow for more target group specific campaign measurements in the future. In combination with persistent frequency sensors, we aim to model real-time pedestrian movements and poster evaluations.

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